

NAME: \_\_\_\_\_

**MATH 12002**

**HOMEWORK #4 (13 pts)**

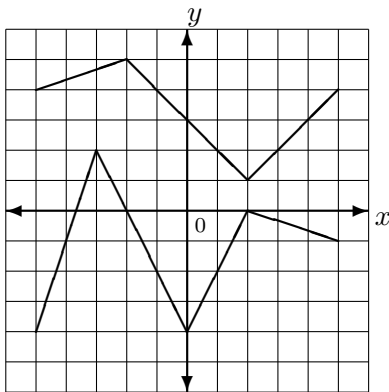
**SPRING 2009**

SHOW ALL WORK FOR FULL CREDIT — PLEASE CIRCLE YOUR FINAL ANSWER

DUE: MONDAY, FEBRUARY 23, 2009 AT THE BEGINNING OF CLASS

NO EXCEPTIONS!!!

1. (2 pts each) The graphs of functions  $f$  and  $g$  are shown below.



- (a) Let  $F(x) = f(x) \cdot g(x)$ . Compute  $F'(-1)$ .

- (b) Let  $H(x) = \sqrt{f(x)} + [g(x)]^2$ . Compute  $H'(-1)$ .

2. (3 pts) Use implicit differentiation to find the slope of the line tangent to the curve

$$x^3 + x^2y + y^2 = 1$$

at the point  $(1, -1)$ .

3. (2 pts) Let  $y$  be a differentiable function of  $x$  satisfying the equation

$$x^3 + x \sin y = \cos x + 3y^2.$$

Use implicit differentiation to find  $y'$ .

4. (2 pts) Let  $f(x) = (3x^2 - 5)^3$ . Find  $f''(1)$ .

5. (2 pts) Find all values of  $x$  (in radians) for which

$$f(x) = \sin^2 x - \sqrt{3} \cos x$$

has a horizontal tangent.