

Definition: Suppose a curve  $C$  in the plane consists of the set of points of the form  $(x, y)$  where

$$x = f(t) \quad \text{and} \quad y = g(t)$$

for some pair of continuous functions  $f$  and  $g$  defined on an interval  $I$ . The equations  $x = f(t)$  and  $y = g(t)$  are said to give a **parametric representation** of  $C$  in the parameter  $t$ .

EXAMPLE 1: Sketch the curve given by  $x = 2t + 1$  and  $y = 4t^2 - 1$  where  $-1 \leq t \leq 1$ .

EXAMPLE 2: Sketch the curve given by  $x = \cos \theta$  and  $y = \sin \theta$  where  $0 \leq \theta \leq 2\pi$ .

EXAMPLE 3: Sketch the curve given by  $x = t^2$  and  $y = t^3$ .

EXAMPLE 4: Sketch the curve given by  $x = \cos t$  and  $y = \cos 2t$ .