# Section 8.2: Multiplication and Division of Integers

## **MULTIPLICATION:**

• **Number line:** Recall that the multiplication of whole numbers can be viewed as repeated addition.

• Pattern:

## • Charge Field: $a \times b$

- 1. Begin with a set of zero.
- 2. If a > 0, then we add a groups of b to our set.
- 3. If a < 0, then we take away |a| groups of b from our set.

**Example 1:** Illustrate  $3 \times -4$  using the charge field method.

**Example 2:** Illustrate  $-5 \times -2$  using the charge field method.

### **INTEGER MULTIPLICATION FACTS:**

- $a \times 0 = 0 = 0 \times a$
- positive  $\times$  negative = negative
- positive  $\times$  positive = positive
- negative  $\times$  negative = positive

#### **Properties of Integer Multiplication**

- Closure Property: integer  $\times$  integer = integer.
- Commutative Property: If a and b are integers, then  $a \cdot b = b \cdot a$ .
- Associative Property: If a, b, and c are integers, then  $a \cdot (b \cdot c) = (a \cdot b) \cdot c$ .
- <u>Identity Property</u>: One is the unique number such that  $a \cdot 1 = a = 1 \cdot a$  for all integers  $\overline{a}$ . We say that 1 is the multiplicative identity.
- Distributive Property: If a, b, and c are integers, then a(b + c) = ab + ac and  $\overline{a(b-c) = ab ac}$ .
- Multiplication Cancellation Property: Suppose  $c \neq 0$ . If ac = bc then a = b.
- Zero Divisors Property: ab = 0 if and only if a = 0 or b = 0.

**DIVISION:** Let a and b be integers with  $b \neq 0$ . Then  $a \div b = c$  if and only if  $a = b \cdot c$  for a unique integer c. (Recall that this is the missing factor approach).

## **INTEGER DIVISION FACTS:**

- $\bullet \ a \div 1 = a$
- positive  $\div$  negative = negative
- positive  $\div$  positive = positive
- negative  $\div$  negative = positive

- negative  $\div$  positive = negative
- If  $a \neq 0$ , then  $0 \div a = 0$
- $a \div 0 =$  undefined
- $0 \div 0 =$  undefined

**Example 3:** Let a be a negative integer, b be a positive integer, and c be a negative integer. Determine if each of the following is positive, negative, or cannot be determined.

(a) (a-b)(b-c) (c) (a+c)(b+c)

(b) 
$$4a - 3b + 9c$$
 (d)  $a + bc$ 

**NEGATIVE EXPONENTS:** Let a be any nonzero number and n be a positive integer. Then

$$a^{-n} = \frac{1}{a^n}$$
 and  $\frac{1}{a^{-n}} = a^n$ .

**Example 4:** Simplify the following:

(a) 
$$(-5)^2 =$$
 (c)  $4^{-2} =$ 

(b) 
$$-6^2 =$$
 (d)  $5^{-3} =$