

In section 9.2 we calculated the surface area of a surface of revolution. In this section, we will calculate the surface area of a surface given by  $z = f(x, y)$ .

**Area of a Surface:** If  $f$  and its first partial derivatives are continuous on the closed region  $D$  in the  $xy$ -plane, then the **area of the surface** given by  $z = f(x, y)$  over  $D$  is given by

$$A(S) = \iint_D \sqrt{1 + [f_x(x, y)]^2 + [f_y(x, y)]^2} \, dA$$

EXAMPLE 1: Find the area of the part of the surface  $z = 1 + 3x + 2y^2$  that lies above the triangle with vertices  $(0, 0)$ ,  $(0, 1)$  and  $(2, 1)$ .

EXAMPLE 2: Find the area of the part of the surface of the paraboloid  $z = 4 - x^2 - y^2$  that lies above the  $xy$ -plane.

**Homework:** pg 1058; 1-9 odd