

## The Edgeworth Box

## The Basic Theorem

- The basic theorem in welfare economics:  
*A market, exchange, economy will achieve efficient resource allocation.*
- We intend to show the basics of that proof.

## Some Basic Assumptions

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## Some Basic Assumptions

- A simple economy: Harry and Sally.
- There are two factors of production, capital, K, and labor, L.  
$$L = L_H + L_S$$
- These two factors of production can be used to produce either apples or bananas.

## Three Basic Questions

- How many apples and how many bananas should be produced?

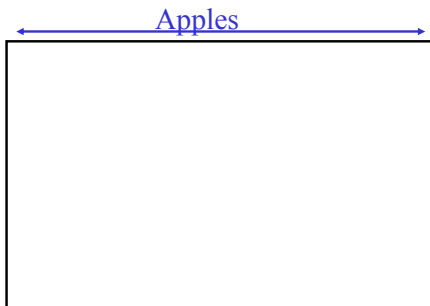
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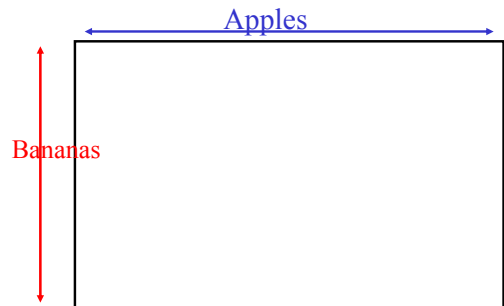
### Three Basic Questions

- How many apples and how many bananas should be produced?
- How should the apples and bananas be allocated between Harry and Sally?
- How should capital and labor be allocated to the production of apples and bananas?

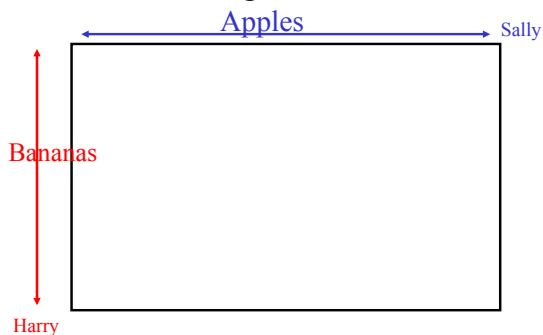
### The Edgeworth Box



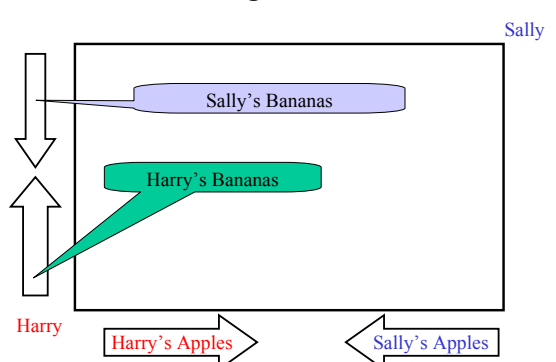
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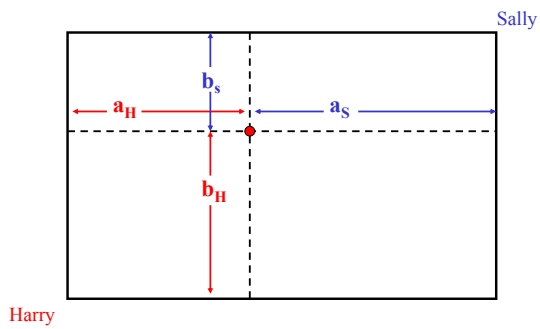
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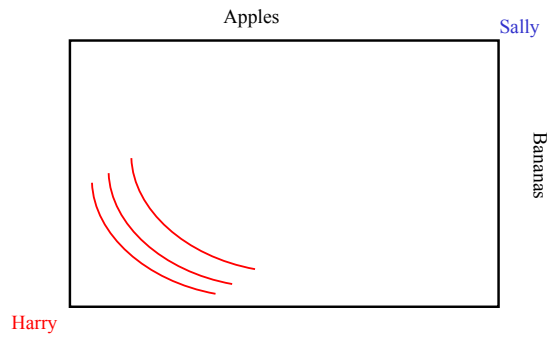
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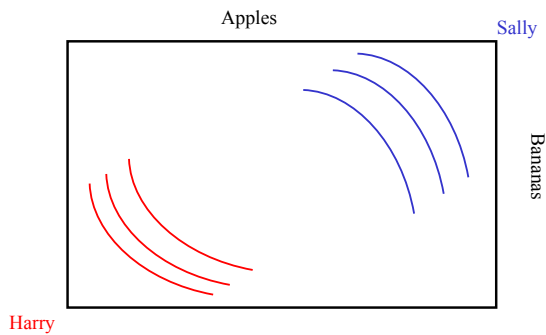
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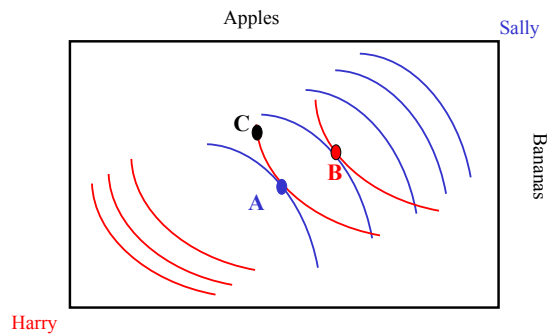
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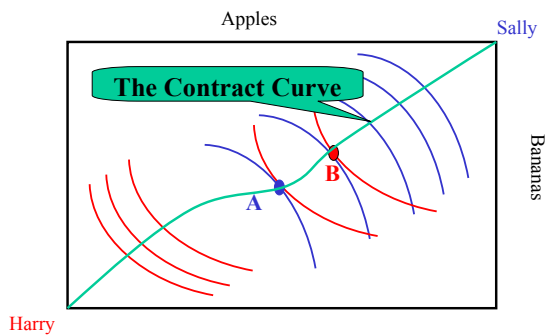
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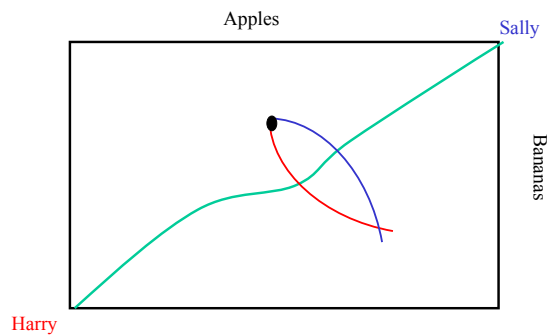
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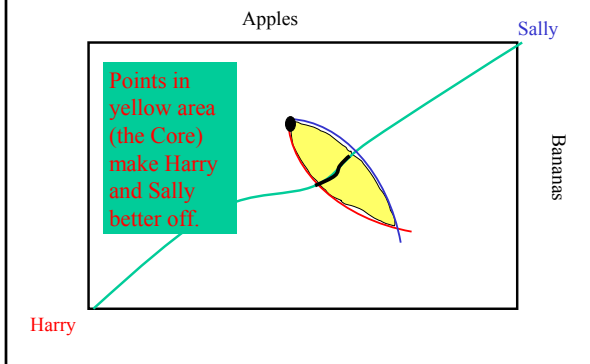
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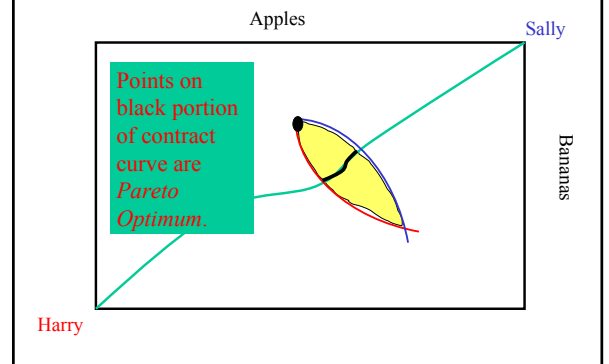
## The Contract Curve



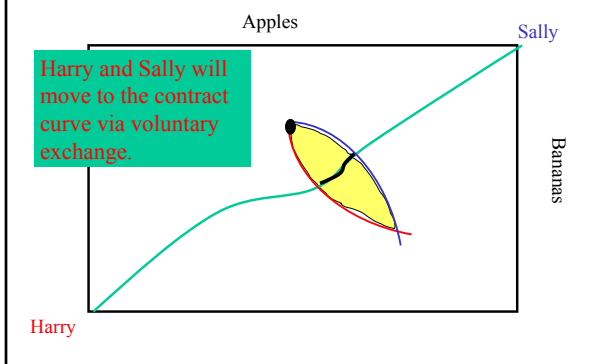
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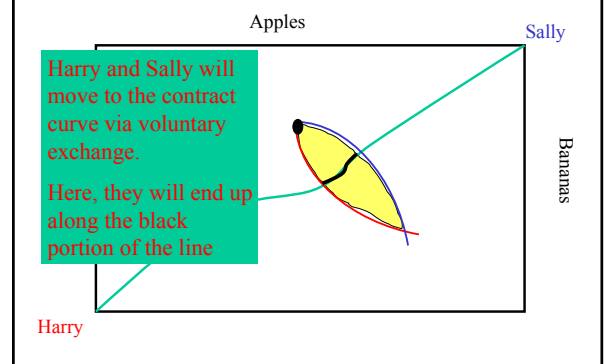
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## Pareto Optimality

- When they are on the contract curve, we say that they have achieved Pareto Optimality, the economist's equivalent of "bliss".

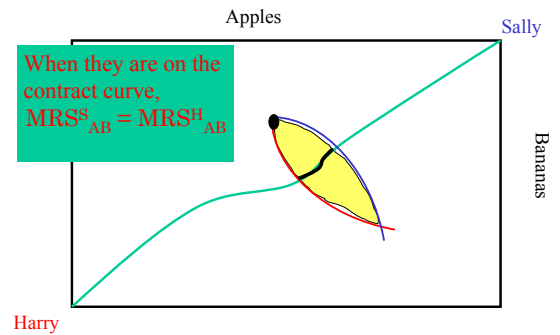
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- It is impossible to make Harry better off without making Sally worse off (or vice versa)

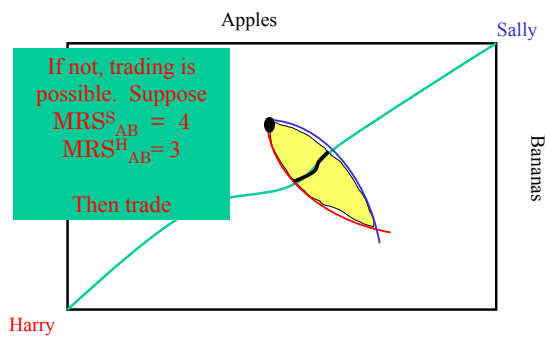
## Pareto Optimality

- When they are on the contract curve, we say that they have achieved Pareto Optimality, the economist's equivalent of "bliss".
- It is impossible to make Harry better off without making Sally worse off (or vice versa)
- If they are not on the contract curve, it is possible to make one or both better off without making the other worse off.

## Marginal Rates of Substitution



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## Two Qualifications

- Consumer Sovereignty

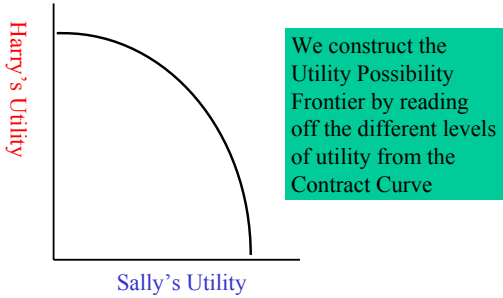
## Two Qualifications

- Consumer Sovereignty
  - Are we comfortable with welfare checks being spend on drugs and alcohol?
  - Do we think children know what is best for them?

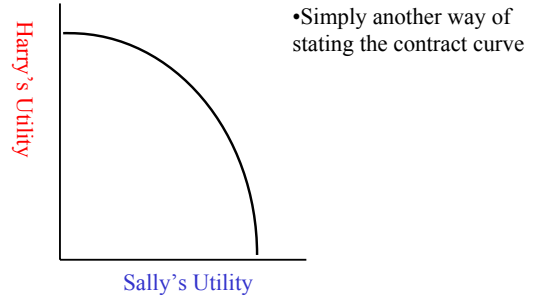
## Two Qualifications

- Consumer Sovereignty
- Do we have anything to say about the right point on the contract curve?

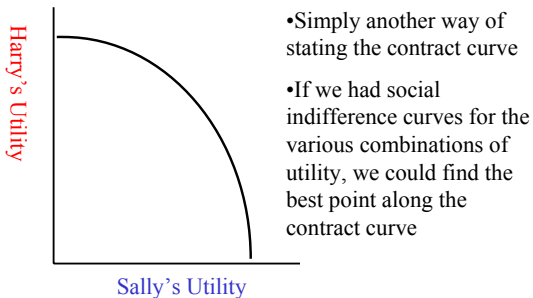
## The Utility Possibility Frontier



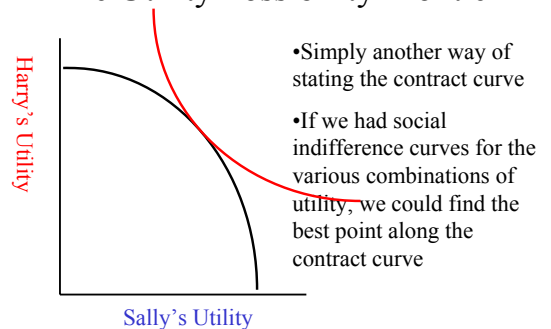
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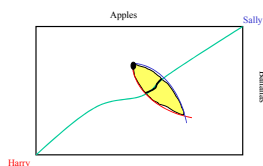


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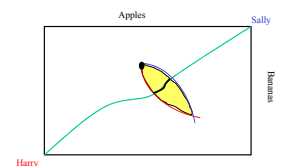
## The Core

- The yellow area is the **core**.



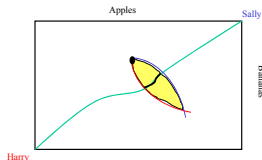
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- If only Harry and Sally are involved, they will sit down and simply haggle with each other.



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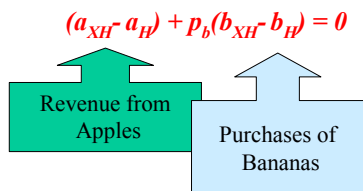
- The yellow area is the core.
- If only Harry and Sally are involved, they will sit down and simply haggle with each other.
- Suppose there are hundreds of Harry's and Sally's?



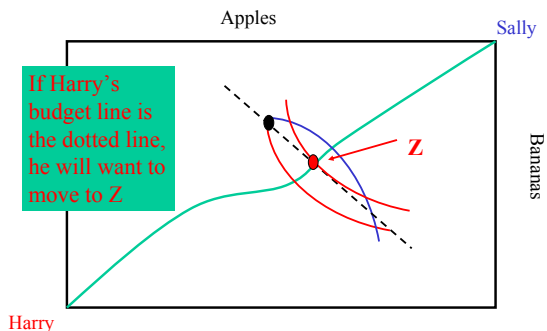
## Markets

- The normal laws of supply and demand will get us to this point.
- Suppose that Harry and Sally start out with apples and bananas given by  $(a_{XH}, b_{XH})$  and  $(a_{XS}, b_{XS})$  respectively.
- We tell Harry that he can buy and sell apples and bananas at prices  $(1, p_b)$ . The only constraint is that  $(a_{XH} - a_H) + p_b(b_{XH} - b_H) = 0$

## Markets



## The Contract Curve



## Markets

- If Sally is told that she can buy and sell apples and bananas subject to a budget constraint  $(a_{XS} - a_S) + p_b(b_{XS} - b_S) = 0$  she will be willing to buy and sell.

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- However** the price that persuaded Harry to move to Z, might or might not move her to Z.

## The Fundamental Theorem

- **For any starting point there is a price  $p_b$  which will lead both Harry and Sally to move to the same point on the contract curve.**

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- For any starting point there is a price  $p_b$  which will lead both Harry and Sally to move to the same point on the contract curve.
- That is, there is a price that equates supply and demand. It puts Harry and Sally on the contract curve

## Summary

- Normal trading gets Pareto Optimality in distribution.

$$MRS(Harry) = MRS(Sally)$$

- More to Come

End

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