

Optimal Inflation

$$r_N = r_R + \eta_e = 0$$

The Optimal Inflation Rate

- The private cost of holding money is r_N
- Economic Efficiency requires setting PC=SC.

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- Economic Efficiency requires setting PC=SC.

$$SC = 0$$

The Optimal Inflation Rate

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The Optimal Inflation Rate

$$r_N = r_R + \eta_e = 0$$

$$\eta_e = -r_R < 0$$

The Optimal Inflation Rate

$$\longrightarrow \eta_e = -r_R < 0$$

$$\eta_e = \frac{\Delta M}{M} - \frac{\Delta Y}{Y}$$

$$\frac{\Delta M}{M} = \frac{\Delta Y}{Y} - r_R < 0$$

The Optimal Inflation Rate

$$\eta_e = -r_R < 0$$

$$\rightarrow \eta_e = \frac{\Delta M}{M} - \frac{\Delta Y}{Y}$$

$$\frac{\Delta M}{M} = \frac{\Delta Y}{Y} - r_R < 0$$

The Optimal Inflation Rate

$$\eta_e = -r_R < 0$$

$$\eta_e = \frac{\Delta M}{M} - \frac{\Delta Y}{Y}$$

$$\rightarrow \frac{\Delta M}{M} = \frac{\Delta Y}{Y} - r_R < 0$$

Conclusion

- A 1% inflation rate costs \cong \$250 million
- Concentrate on price stability

Uncertainty Costs

- Suppose next year's inflation rate is equally likely to be three, six, or nine percent.

$$P(3\%) = \frac{1}{3}$$

$$P(6\%) = \frac{1}{3}$$

$$P(9\%) = \frac{1}{3}$$

Production

- The CEO of Acme Widgets must price the product a year in advance.

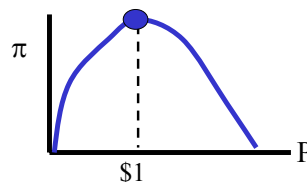
$$P(3\%) = \frac{1}{3}$$

$$P(6\%) = \frac{1}{3}$$

$$P(9\%) = \frac{1}{3}$$

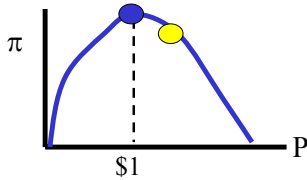
Production

- If the inflation rate turns out to be exactly six percent, the right price would be \$1.00 each.



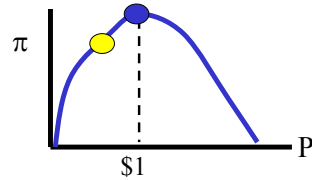
Production

- If the inflation rate turns out to be 3%, he will have overpriced.



Production

- If the inflation rate turns out to be 9%, he will have under priced.



Production

- If the inflation rate turns out to be 3 percent, the right price would be too high, and widgets would be priced 3% too high and both demand and profits will suffer.
- If the inflation rate turns out to be 6 percent, the right price would be just right, and widgets would be priced just right, and both demand and profits will be maximized.
- If the inflation rate turns out to be 9 percent, the right price would be too low, and widgets would be priced 3% too low and both demand and profits will suffer.

If the uncertainty can be ended, Acme can make more money.

At 3%, $\pi = \$70$

At 6%, $\pi = \$100$

At 9%, $\pi = \$70$

Optimal Inflation

Production

- If the inflation rate turns out to be 3 percent, the right price would be too high, and widgets would be priced 3% too high and both demand and profits will suffer.
- If the inflation rate turns out to be 6 percent, the right price would be just right, and widgets would be priced just right, and both demand and profits will be maximized.
- If the inflation rate turns out to be 9 percent, the right price would be too low, and widgets would be priced 3% too low and both demand and profits will suffer.

$$E(\pi) = \frac{1}{3}\$70 + \frac{1}{3}\$100 + \frac{1}{3}\$70 = \$80$$

Optimal Inflation

Production

- If the inflation rate turns out to be 0 percent, the right price would be too high, and widgets would be priced 3% too high and both demand and profits will suffer.
- If the inflation rate turns out to be 6 percent, the right price would be just right, and widgets would be priced just right, and both demand and profits will be maximized.
- If the inflation rate turns out to be 12 percent, the right price would be too low, and widgets would be priced 3% too low and both demand and profits will suffer.

If no uncertainty, $\pi = \$100$

Optimal Inflation

Extra Uncertainty

Suppose

$$P(0\%) = \frac{1}{3}$$

$$P(6\%) = \frac{1}{3}$$

$$P(12\%) = \frac{1}{3}$$

At 0%, $\pi = \$50$

At 6%, $\pi = \$100$

At 12%, $\pi = \$50$

Optimal Inflation

Extra Uncertainty

Suppose

$$P(0\%) = \frac{1}{3}$$

At 0%, $\pi = \$50$

$\frac{1}{3}$

At 6%, $\pi = \$100$

$$E(\pi) = \frac{1}{3}\$50 + \frac{1}{3}\$100 + \frac{1}{3}\$50 = \$67$$

$$P(12\%) = \frac{1}{3}$$

At 12%, $\pi = \$50$

Extra Uncertainty

Suppose

$$P(0\%) = \frac{1}{3}$$

At 0%, $\pi = \$50$

$$P(6\%) = \frac{1}{3}$$

Moral: the greater the uncertainty, the greater the chance you have made a mistake that costs you money.

$\pi = \$100$

$$P(12\%) = \frac{1}{3}$$

$\pi = \$50$

End

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