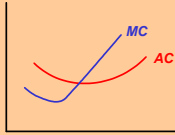


## Marginal and Average Cost



## A Cost Function

Quantity	Total Cost	Average Cost	Incremental Cost or Marginal Cost
0	11		
1	14		
2	24		
3	36		
4	52		
5	75		

## Average Cost

Quantity	Total Cost	Average Cost	Incremental Cost or Marginal Cost
0	11		
1	14		
2	24	12	
3	36		
4	52		
5	75		

## Average Cost

Quantity	Total Cost	Average Cost	Incremental Cost or Marginal Cost
0	11	NA	
1	14	14	
2	24	12	
3	36	12	
4	52	13	
5	75	15	

## Marginal Cost

Quantity	Total Cost	Average Cost	Incremental Cost or Marginal Cost
0	11	NA	
1	14	14	
2	24	12	10
3	36	12	
4	52	13	
5	75	15	

## Marginal Cost

Quantity	Total Cost	Average Cost	Incremental Cost or Marginal Cost
0	11	NA	
1	14	14	3
2	24	12	10
3	36	12	12
4	52	13	16
5	75	15	23

## A Key Proposition

- If  $MC < AC$ , AC is falling

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- If  $MC < AC$ , AC is falling
- If  $MC = AC$ , AC is constant

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- If  $MC > AC$ , AC is rising

## A Key Proposition

- If  $MC < AC$ , AC is falling
- If  $MC = AC$ , AC is constant
- If  $MC > AC$ , AC is rising
- Intuitively, the only way AC can be rising is if the incremental units cost more than the average.

## The Proposition Illustrated

Quantity	Total Cost	Average Cost	Incremental Cost or Marginal Cost
0	11	NA	
1	14	14	3
2	24	12	10
3	36	12	12
4	52	13	16
5	75	15	23

## MC < AC; AC Falling

Quantity	Total Cost	Average Cost	Incremental Cost or Marginal Cost
0	11	NA	
1	14	14	3
2	24	12	10
3	36	12	12
4	52	13	16
5	75	15	23

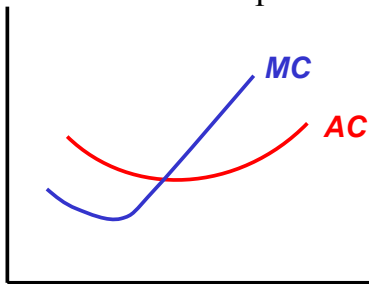
### MC > AC; AC Rising

Quantity	Total Cost	Average Cost	Incremental Cost or Marginal Cost
0	11	NA	
1	14	14	3
2	24	12	10
3	36	12	12
4	52	13	16
5	75	15	23

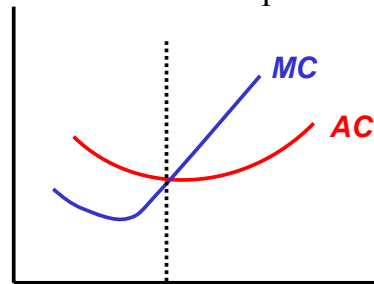
### MC = AC; AC Constant

Quantity	Total Cost	Average Cost	Incremental Cost or Marginal Cost
0	11	NA	
1	14	14	3
2	24	12	10
3	36	12	12
4	52	13	16
5	75	15	23

### The Graph



### The Graph



### The Mathematics

$$AC = \frac{C(q)}{q}$$

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$$\frac{dAC}{dq} = \frac{dC}{dq} \left( \frac{1}{q} \right) - C(q) \left( \frac{1}{q^2} \right)$$

## The Mathematics

$$AC = \frac{C(q)}{q}$$

$$\frac{dAC}{dq} = \frac{dC}{dq} \left( \frac{1}{q} \right) - C(q) \left( \frac{1}{q^2} \right)$$

$$\frac{dAC}{dQ} = \left( \frac{1}{q} \right) \left( \frac{dC}{dq} - \frac{C(q)}{q} \right)$$

## The Mathematics

$$\frac{dAC}{dQ} = \left( \frac{1}{q} \right) \left( \frac{dC}{dq} - \frac{C(q)}{q} \right)$$

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$$\frac{dAC}{dQ} = \left( \frac{1}{q} \right) \left( \frac{dC}{dq} - \frac{C(q)}{q} \right)$$

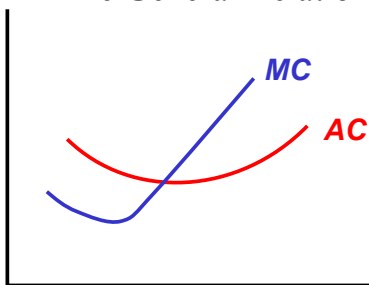
$$\frac{dAC}{dQ} = \left( \frac{1}{q} \right) (MC - AC)$$

## The Mathematics

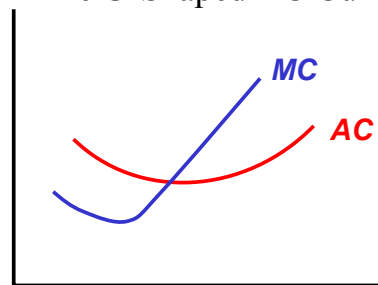
$$\frac{dAC}{dQ} = \left( \frac{1}{q} \right) (MC - AC)$$

If  $MC > AC$ , AC is rising;  
If  $MC < AC$ , AC is falling

## The General Relation



## The U-Shaped AC Curve



## The U-Shaped AC Curve

, *MC*

This is an empirical statement, not a general requirement  
Let's defer the question of why this relation until later.

End

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